

Protein structure mining using a structural alphabet

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ABSTRACT

We present a comprehensive evaluation of a new structure mining method called PB-ALIGN. It is based on the encoding of protein structure as 1D sequence of a combination of 16 short structural motifs or protein blocks (PBs). PBs are short motifs capable of representing most of the local structural features of a protein backbone. Using derived PB substitution matrix and simple dynamic programming algorithm, PB sequences are aligned the same way amino acid sequences to yield structure alignment. PBs are short motifs capable of representing most of the local structural features of a protein backbone. Alignment of these local features as sequence of symbols enables fast detection of structural similarities between two proteins. Ability of the method to characterize and align regions beyond regular secondary structures, for example, N and C caps of helix and loops connecting regular structures, puts it a step ahead of existing methods, which strongly rely on secondary structure elements. PB-ALIGN achieved efficiency of 85% in extracting true fold from a large database of 7259 SCOP domains and was successful in 82% cases to identify true super-family members. On comparison to 13 existing structure comparison/mining methods, PB-ALIGN emerged as the best on general ability test dataset and was at par with methods like YAKUSA and CE on nontrivial test dataset. Furthermore, the proposed method performed well when compared to flexible structure alignment method like FATCAT and outperforms in processing speed (less than 45 s per database scan). This work also establishes a reliable cut-off value for the demarcation of similar folds. It finally shows that global alignment scores of unrelated structures using PBs follow an extreme value distribution. PB-ALIGN is freely available on web server called Protein Block Expert (PBE) at <http://bioinformatics.univ-reunion.fr/PBE/>.

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Key words: substitution matrix; protein blocks; local protein structure; structure mining; local alignment; global alignment; structure comparison.

INTRODUCTION

Protein Data Bank (PDB)¹ offers to date more than 43,000 protein structures in the public domain. This data encloses wealth of information, which plays a critical role in our understanding of protein function, its evolution and sequence to structure relationship that further unfolds improved solutions to structure prediction and validation. Mining of information from this huge amount of data plays a crucial role, and most of the time, the information includes the measure of structural similarities between two or more proteins. Steady increase in number of known proteins has made it impossible for manual inspection of each and every protein present in PDB with rare exception of SCOP² database based on manual classification of protein domains. To overcome this limitation, many groups have developed various structure comparison methods.^{3,4}

Structure comparison between two proteins has been of major interest from the time when Pertuz⁵ used structure alignment to highlight structural similarities between myoglobin and hemoglobin despite sharing low sequence similarities. Common functionality between these two proteins is not accidental; evolutionary relationship and shared structural features are the reasons that describe the above phenomena. Structure comparison methods are aimed to find these structural similarities to foresee protein's function, especially at low sequence

Abbreviations: PBs, protein blocks; SSEs, secondary structure elements; SA, structural alphabet; LA, local alignment; GA, global alignment; PBE, protein block expert; rmsd, root mean square deviation; EVD, extreme value distribution.

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similarity, to study evolutionary relationship and basic understanding of protein-folding problem.

Furthermore, comparison and alignment help in organization and classification of known proteins,^{6,7} mining of similar known proteins for newly solved structure,^{8–11} identification of functionally important sequence pattern in homologous proteins,^{12,13} and they also provide point of reference for sequence alignment methods.^{14–16} Structure comparison and alignment is a more challenging and complicated problem due to a number of reasons. First problem is about what to compare? Once this decision is made, it is very difficult to obtain optimal alignment or identify among many alignments, as there are number of ways to align two structures. Also, in presence of high structural similarity, it is challenging to make out if it arises from evolutionary constraint or is just an analogy due to physical constraint on fold space.

There are various methods for structure comparison based on what level the structure is represented; some methods use all atom model, but are limited to small substructures¹⁷; more common approach involves backbone comparison of two proteins based on backbone atoms, for example, C α atom or internal distance matrices^{9,18,19} or internal angles^{10,20,21} estimated from backbone atoms. Alignment of structures based on initial alignment of secondary structure elements (SSEs) and further refinement through iteration is also a commonly used approach.^{11,22,23} Graph theory-based SSE alignments provide another alternative solution for structure comparison.^{24,25} Methods using backbone coordinates for structure comparison relies on root mean square deviation measure between two proteins, and objective function has to minimize this value to identify structural similarities. Such methods^{26–28} are useful for comparing two proteins or substructures, but they are computationally expensive, making them too slow for mining of similar structures from large database. Recently developed methods like FlexProt²⁹ and FATCAT³⁰ use flexible structure alignment approach by introducing twists between aligned fragment pairs to improve overall superposition and try to overcome the limitations of rigid body structure alignment techniques.

Popular methods like DALI,⁹ SSAP,¹⁹ and CE¹⁸ use reduced representation of protein backbone in terms of distance matrices. DALI uses hexapeptide distance matrices combined with dynamic programming and Monte Carlo optimization technique to obtain global alignment (GA). The combinatorial extension (CE) method combines aligned short structural fragments into larger alignment paths and apply dynamic programming to generate GA. Both these methods are most commonly used for structure comparison and fast structure mining, though sometimes absence of homolog in database can increase search time considerably.

Most of these methods perform structure alignment based on SSEs or use them to obtain initial starting

point. Protein structures can also be approximately described using structural alphabets (SAs), which are recurring short structural motifs found across protein 3D space (for a review, see Offmann *et al.*³¹). Many groups have identified these recurring short motifs capable of describing protein backbone^{32–34} and are believed to be more informative in protein structure analysis.³⁵

Use of SAs for structure comparison has been attempted only in the last decade. 3D-Blast is an example of one such recently developed approach, which uses a 23-state SA to describe the backbone.³⁶ This method uses BLAST as a search method using a SA substitution matrix to find the longest common substructures with high-scoring segment pairs. It uses the *E*-value of BLAST as measure of statistical significance of an alignment and generates results with performance comparable to known methods.

Using a set of 16 pentapeptide structural motifs known as protein blocks (PBs),^{37,38} we have introduced a new methodology of analyzing protein structures.³⁹ Each of these 16 motifs is represented by character alphabets (*a, b, c, . . . , p*) and are described by vector of eight dihedral angles (ϕ, ψ) making it possible to represent 3D protein structure by a string of 1D sequence of PBs. Taking advantage of this reduced representation of protein structure as mere sequence of symbols, we recently derived a PB substitution matrix and investigated its potential utility in protein structure analysis^{31,39} or for discovering functional local structural motifs.⁴⁰

A new structure comparison method (PB-ALIGN) useful for mining protein structural databases has been developed. This approach is based on PB sequence alignment using the newly derived PB substitution matrix, which has been developed.³⁹ The basic premise of structure alignment is very simple and is based on encoding of protein backbone by a sequence of characters representing PBs. Further, these PB sequences are aligned just like amino acid sequences using dynamic programming combined with a substitution matrix. Capability of PBs to represent local structure variations and alignment of these PBs provides more intuitive knowledge of structurally similar regions in two proteins when compared to SSE representation. Structure alignment based on PB sequence is not only able to align regular substructures but also the N and C cap regions. It also highlights structural variations in loops that connect regular secondary structures. PB sequence alignment to obtain structure alignment is a very fast procedure of structure mining and allows large database mining in real time.⁴¹

In the present study, we provide a comprehensive evaluation of the methodology compared to existing techniques. We also provide more thorough analysis of the efficiency rate of mining proteins from a large database, using PBE server. In addition, we present optimal gap penalty for both local⁴² and global⁴³ alignment techniques. Our results show that PB-ALIGN provides

equivalent or better efficiency rate in mining of structures from large database when compared to methods like DALI,⁹ CE,¹⁸ and FATCAT³⁰ and is much faster in all of them. Our method achieved 89% success rate in extracting true fold from pairwise alignment of 7259 against 7259 SCOP domains. In non-trivial cases, PB-ALIGN provides comparable results to more robust and complex methods and also gave satisfactory results while handling multidomain protein. We addressed the question of alignment score threshold for making decision that two aligned structures correspond to same fold. The statistical characteristics of the distribution of GA scores were finally examined.

MATERIALS AND METHODS

Dataset used for evaluation of PB-ALIGN

In the present study, we have used batteries of test dataset to assess the performance PB-ALIGN in different experimental conditions. Database of 7259 SCOP (v1.65) domains filtered at 95% identity implemented in PBE web server⁸ are used for assessing the mining efficiency of the method. Distribution of seven SCOP classes is as follows: 1337 (18.5%) α domains, 2077 (28.6%) β domains, 1387 (19.0%) $\alpha\beta$ domains, 1529 (21.0%) $\alpha + \beta$ domains, 700 (9.6%) small domains, 89 (1.2%) multidomains, and 140 (1.9%) membrane domains. PB-ALIGN was compared with 13 existing structure mining/comparison methods based on three different datasets. The general ability of the methods to extract similar structure proteins was tested on 61 query proteins belonging to ten protein families, representing the four CATH main classes (mainly α , mainly β , mixed $\alpha\beta$, and few secondary structures). Same dataset was used in two independent studies done by Novotny *et al.*³ and Carpentier *et al.*¹⁰ Ability of the methods to handle multidomain proteins was evaluated based on two multidomain queries selected by same groups. Fourteen nontrivial query-target pairs were taken from study done by Carpentier *et al.*¹⁰ to test the robustness of the method in detecting difficult structural similarities. Furthermore, we performed comparison of PB-ALIGN with flexible structure alignment program FATCAT, based on pairwise alignment of 10 difficult pairs as used by Ye *et al.*³⁰

Encoding 3D structures into PB sequence

Local backbone features of a protein can be represented by 16 prototypes of five-residue long motifs called PBs.³⁸ Each PB is characterized by vector of eight dihedral (ϕ , ψ) angles associated with five consecutive C α atoms, and the 16 PBs are denoted by a character set varying from *a* to *p*. Encoding of protein backbone into PB sequence is a two-step process: (i) coordinates of backbone atoms are used to calculate sequence of (ϕ , ψ)

angles; (ii) an overlapping window of eight (ϕ , ψ) angles (corresponding to five C α residues) is moved along the backbone. PBs for each window is assigned on the basis of smallest dissimilarity measure called root mean square deviation on angular values or rmsda⁴⁴ calculated between observed (ϕ , ψ) values in the window and the standard dihedral angles for various PBs. By following the above simple procedure, a 3D structure of a protein can be encoded into a 1D sequence of PBs representing local structural information as sequence of SAs.

PB substitution matrix

A 16 \times 16 PB substitution matrix has been recently derived by our group.⁴⁵ The substitution scores between PBs were evaluated by counting the number of substitutions occurring in conserved regions of structurally aligned homologous proteins. These proteins are selected from large database, PALI,^{46,47} containing structure-based pairwise and multiple alignments of homologous proteins of known three-dimensional structures. The database uses a rigid-body superposition program, STAMP,⁴⁸ to generate structure-based alignments. In total, 21,503 pairwise alignments from 1197 SCOP families were analyzed, which accounted for more than 2,000,000 PB substitutions. The raw frequencies are normalized and expressed as the log-odds score. The obtained scores provide extent of preference of a PB in a protein for its retention or substitution and allow evaluating equivalence between homologous structures. The matrix has been validated in our previous studies and has been shown to be useful in identification of structurally equivalent regions in two proteins. In addition, the matrix has potential applications in differentiating between conformational differences and rigid body shifts among homologous protein structures.⁴⁵

Gap penalty optimization

In our previous study, we selected an arbitrary gap penalty of -0.5 on manual inspection of PB alignments. Here, we follow extensive procedure to suggest optimal gap penalties. Penalty optimization procedure is based on two criteria: effect of gap penalty on overall mining efficiency of similar structure proteins and quality of alignments generated. Structure mining efficiency is measured by counting number of times a true hit at class, fold, super-family, and family level is obtained when Top 10, 5, and first ranking alignments are considered for a given query. Quality of alignment is measured in terms of rmsd value obtained from superimposition of protein pairs based on PB alignment. Superimposition is performed using ProFit⁴⁹ software, where equivalent zones are specified by PB alignment.

We performed a comprehensive study to suggest optimal gap penalty for both local alignment (LA) and GA

Table I
Optimization of Global Gap Penalty

	Level/gap penalty					
	-0.5	-1.0	-2.0	-2.5	-3.0	-5.0
Class	98.1	97.9	97.9	97.95	98.05	97.9
Fold	66.35	66.55	66.9	66.5	66.25	63.85
Super-family	61.5	61.65	61.65	61.35	61.05	58.7
Family	55.5	55.95	56.6	56.6	56.2	54.45

Effect of gap penalty on mining rate at class, fold, super-family, and family level for global alignment. The results are from top 10 ranking alignments. Analysis was performed on 2000 randomly selected SCOP domains.

algorithms using 2000 randomly sampled domains. A database of 2000×2000 pairwise PB alignments was generated to perform above two analyses. Attention was given to keep the relative proportion of seven major classes similar to that in original databank. Jackknife approach was used to measure mining efficiency, and alignment quality measure was done by considering only pairs belonging to same family. For GA of PB sequences, we used following set of gap penalties -0.5 , -2.0 , -2.5 , -3.0 , and -5.0 , and optimal gap penalty for LA algorithm was selected from the following set of penalties -0.5 , -2.0 , -3.0 , -5.0 , and -7.0 .

RESULTS AND DISCUSSION

Effect of gap penalty on mining similar protein structures

Using 2000 randomly sampled domains, we assessed efficiency of both local and GA techniques to extract structurally similar proteins at class, fold, super-family, and family levels for a given gap penalty. For a given query, hits are calculated by considering Top 10, 5, and first ranking alignments. In the following analysis, we present results from Top 10 ranking alignments.

Table I reports efficiency rate for mining proteins at class, fold, super-family, and family level considering Top 10 ranking alignments based on GA algorithm. Bold values indicate best efficiency rate achieved at each level. With varying gap penalty from -0.5 to -3.0 , negligible effects on efficiency of extraction of proteins was detected. Not more than 0.6% of change was seen in efficiency rate in this range of gap penalties. Further increase reduces the efficiency of the method by almost 3% as illustrated from low success rate achieved at a penalty of -5.0 . Among penalties used in this analysis, gap penalty of -2.0 seems to give the best results, though performance was not very much higher for other penalties used.

Table II shows the success rate of mining similar proteins using LA at class, fold, super-family, and family level when Top 10 ranking alignments are taken into account. Because of the basic nature of the algorithm, it

was suspected that the higher gap penalty will yield better results and efficiency rate can be inferior to GA. Indeed the two assumptions are true from the above tables. Efficiency rate has increased by almost 10% at fold level by changing penalty from -0.5 to -2.0 , but overall success rate is slightly lower when compared to GA results. One of the reasons for low efficiency compared to GA can be due to the dataset used in our analysis. Since we have taken well-defined domains as query against well-defined domain database, GA has an advantage here due to the basic nature of the algorithm. This advantage can be a limiting factor for GA in case we use complete protein chains as query without any knowledge of domain boundary. Indeed this is further documented in the following sections where LA outperforms in real case scenario and is able to extract true domains with high scores from the database, whereas GA fails due to more number of gaps introduced in the alignment. On varying penalty from -2.0 to -7.0 , the variation on efficiency rate is very moderate, though best results are obtained at -3.0 or -5.0 gap penalty.

Similar efficiency rates achieved by neighboring gap penalties, both in local and GA techniques indicate variation in gap penalty increases or decreases success rate only to certain extent. No clear favorable gap penalty can hence be considered as optimal. From manual inspection of alignments obtained from various penalties indicated even though mining rate is somewhat constant, gap penalty can have more impact on quality of alignment produced. Based on this assumption, we further studied the relationship between gap penalty and quality of alignment in the following section.

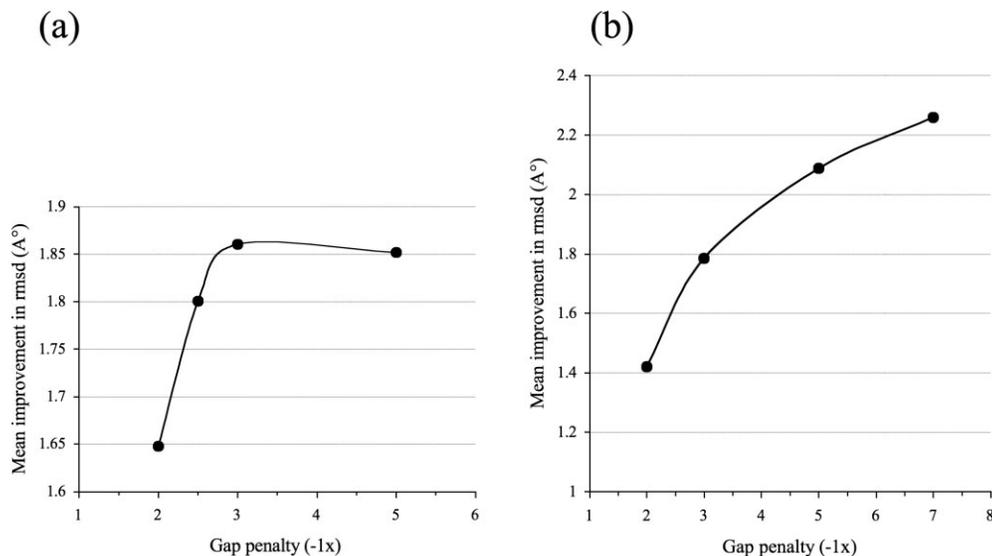
Effect of gap penalty on structural alignment quality

In this analysis, we performed a very simple exercise whereby, for each gap penalty, we generated both local and GAs between pairs of homologous structures belonging to the same family. To assess the quality of PB-based alignments, we used rmsd values from the superimposition of aligned residues. Each PB alignment was

Table II
Optimization of Local Gap Penalty

	Level/gap penalty				
	-0.5	-2.0	-3.0	-5.0	-7.0
Class	89.9	93.3	93.9	94.2	94.25
Fold	50.55	60.55	62.9	62.75	61.35
Super-family	49.15	58.15	60	60	59.05
Family	44.45	52.95	54.1	53.95	52.8

Effect of penalty on mining rate at class, fold, super-family, and family level. Results are from top 10 ranking alignments. Analysis was performed on 2000 randomly selected SCOP domains.

**Figure 1**

Effect of gap penalty on (a) global alignment and (b) local alignment. Figure gives the mean improvement (decrease) in rmsd value (Y axis) at different negative gap penalties (X axis) with respect to rmsd values at a gap penalty of -0.5 . As shown, with increase in negative penalty, there is an improvement in superimposed rmsd values compared to values obtained at a penalty of -0.5 . In case of local alignment (b), there is large improvement in alignment quality as negative gap penalty is increased. Even though -7.0 gives better mean improvement in rmsd, -5.0 was chosen as the desired penalty as a balance between alignment quality and mining efficiency.

converted into corresponding amino acid (AA) alignment and was presented to ProFit software, which further performed least square fit of backbones based on AA alignment. List of rmsd values for every pair was compiled at different gap penalties. For comparison of overall effect of gap penalty on rmsd values, we plotted the average improvement in rmsd values on different gap penalties with respect to rmsd values obtained at penalty of -0.5 . Basically, we have tried to highlight the change (decrease) in rmsd values of various pairs at different gap penalties when compared to values obtained at gap penalty of -0.5 . Figure 1(a) shows the increase in improvement of average rmsd values at different gap penalties (-2.0 , -2.5 , -3.0 , and -5.0) for GA algorithm. From the above figure, it is very clear that increase in negative gap penalty has shifted more number of pairs toward lower rmsd values. For example, on varying gap penalty from -0.5 to -3.0 , almost 18% of alignment pairs have lower rmsd values in interval of 0.5 to 1 Å, and gap penalty of -3.0 and -5.0 has brought improvement of 1 Å or more to almost 44 and 47% homologous pairs, respectively (data not shown). Figure 1(b) shows similar improvement in LA quality by varying gap penalty from -0.5 to -7.0 . Once again overall improvement in rmsd values is seen at various gap penalties. Most fruitful penalties were -5.0 and -7.0 , where average improvement of more than 2 Å is observed.

Based on efficiency of mining similar proteins and improvement in quality of alignment at various penalties

level, it was found that -3.0 and -5.0 were optimal gap penalties for global and LA algorithm, respectively. For GA, penalty of -2.0 yielded best results for extraction of similar proteins, but gap penalty of -3.0 was optimal value in terms of overall alignment quality and mining rate. In case of LA algorithm, even though gap penalty of -7.0 was able to give better rmsd values, the extraction rate was inferior to the penalty of -5.0 by almost 1%, and hence -5.0 was chosen as optimal penalty having balanced results for both alignment quality and mining of proteins.

Mining of protein structures

Efficiency of PB-ALIGN method to extract structurally similar proteins at different SCOP classification level was tested in the following study. We have analyzed 7251 domains selected from SCOP data bank filtered at 95% identity and performed all-against-all pairwise GA of PB sequences with an optimized gap penalty of -3.0 . A class confusion matrix has been generated from 7259×7259 pairwise alignments to assess discriminatory power of simple PB alignments to assign correct SCOP class. The method was evaluated by counting if the true class, fold, super-family, or family member is present within Top 10 hits, ranked by normalized score. It is noteworthy that performance of PB-ALIGN was evaluated in a jack-knife/leave-out approach, where each query domain was removed from database prior to testing. This corresponds

Table III*Efficiency Rate of Mining Proteins at Various SCOP Classification Levels*

SCOP level	Only query domain is removed from database			Whole family related to query is removed from database		
	Top 10	Top 5	Top 1	Top 10	Top 5	Top 1
Class	99.1 (7194)	96.8 (7028)	93.1 (6758)	92.5 (6716)	88 (6394)	76.1 (5529)
Fold	87.4 (6343)	85.6 (6217)	81.3 (5906)	62.6 (4548)	57.5 (4178)	47.4 (3438)
Super-family	84.3 (6122)	82.8 (6011)	79.0 (5739)	65.1 (4727)	60.8 (4412)	53.0 (3846)
Family	80.0 (5809)	78.7 (5714)	75.1 (5453)	n/a	n/a	n/a

Results are reported for top 10, 5, and 1st ranking alignments. Two situations were distinguished; one where only the query is removed from the database and another where the whole family was removed from the database. Values are given as percentage.

n/a: not applicable.

to real-life situations when one will have to query structural databases for mining similar folds. It is also this standard that is largely used for evaluation performance of structure mining methods.^{3,4,9,10,50} However, so as to evaluate efficiency of PB-ALIGN to assign high classification levels and capture remote homology, we also evaluated the situation where members from same family as query were removed. So the dataset size used in all cases dynamically changed depending upon the query protein.

Table III summarizes the results obtained for each level, mainly class, fold, super-family, and family at three different ranks, 1st, 5th, and 10th. True class of a query protein can be found with an efficiency rate ranging between 92.5% and 99.1% when first 10 ranked alignments were considered. Possibility of finding true fold among Top 10 hits showed distinct performance with a hit rate of 62.6% when whole family is jack-knifed and 87.4% when only query is left-out and similar performance were observed at super-family level. Taking into account only the first hit (Top 1 column in Table III), we found between 76.1% and 93.1% success in finding true class. Among these first ranked hits, about 81.3% was from same fold when only query was jack-knifed but of 47.4% when whole family was removed. Similar performance was obtained at super-family level (53%–79%). Finally, on average, one is able to find true family of protein in 80% of cases.

It is further evidenced from our results that, when higher level is properly identified, the chance to identify subsequent lower level is still very good. The biggest decrease in prediction efficiency is observed between class and fold levels. However, it is noteworthy that because we look only at Top 10 or Top 1 for performance evaluation, in some instances, for example, the query d1g73a_ from scop family a.7.4.1, the good hit is found only at lower rank, here at 69th rank because top scores were populated with redundant hits from homologous members of other folds (e.g., 23 hits from a.1.1.2. family, 14 hits from a.1.1.3 family, etc.).

These overall results indicate that mining similar structures using simple PB alignment methodology is performing reasonably well for identifying class and super-family relationships despite the presence of confusion across fold alignments. Indeed, when whole family was left-out, structural relationship at fold level was more difficult to capture using PB-ALIGN when compared to other structural levels. This highlights the importance of quality of information and its coverage in the databases used for mining structures. However, in real life situations, users of structure mining tools such as PB-ALIGN generally expect that their structures be compared to whole PDB or representatives from all families. Hence, overall result presented in Table III is useful to assess how the method is performing when a query has a counterpart from the same family in the PB-ALIGN database. It also shows that the method is able to capture higher-levels relationship (super-family or fold) to some extent when the query has no homologs in the database. These encouraging results demonstrate the feasibility of the method to be useful in projects like structural genomics.

What Table III does not tell us is how much confusion exists between SCOP classes due to reduced representation of 3D structure using PB alignment. To address this question, a class confusion matrix was generated, using a 7259×7259 pairwise alignment, as shown in Table IV. It is important to analyze this confusion because by using 1D PB representation some topological information maybe lost and it becomes crucial for proteins sharing similar succession of SSEs. Again both situations where query-only or whole family related to query is removed from the database were analyzed.

As shown in Table IV, β class was most efficient (89.3%–96.5%) to identify itself, closely followed by α and $\alpha\beta$ class, which have efficiency rates of 83.7%–95% and 83.8%–95.7%, respectively. $\alpha + \beta$ class was found to be confused with other classes with a 88.6% success rate when only query was left-out and a 56.4% rate when family was jack-knifed. Almost half of the false hits from $\alpha + \beta$ are confused with $\alpha\beta$ class. Overlap between $\alpha\beta$

Table IV
Class Confusion Matrix

True class vs. hit class	α	β	$\alpha\beta$	$\alpha + \beta$	MultiDom ^a	Membrane	Small	Total
α	1271 (95.0%)	1	12	12	0	35	6	1337
	1120 (83.7%)	5	47	53	4	88	20	
β	2	2005 (96.5%)	10	36	0	3	21	2077
	3	1855 (89.3%)	20	120	2	18	59	
$\alpha\beta$	7	8	1328 (95.7%)	39	3	0	2	1387
	31	20	1163 (83.8%)	145	20	3	5	
$\alpha + \beta$	34	40	77	1356 (88.6%)	4	3	15	1529
	99	189	301	863 (56.4%)	22	4	50	
MultiDom	3	2	11	2	70 (78.6%)	0	1	89
	6	5	50	9	18 (20.2%)	0	1	
Membrane	29	6	0	2	0	102 (72.8%)	1	140
	64	17	0	4	0	53 (37.8%)	2	
Small	23	24	3	20	0	1	629 (89.8%)	700
	53	115	5	69	0	1	457 (65.3%)	
Total								7259

^aMultiDom corresponds to multidomain protein class.

Matrix gives the efficiency of the method to find true class at first rank and the confusion rate between SCOP classes. Results were generated from 7259 × 7259 pairwise PB alignments. True classes are featured horizontally and predicted classes vertically. Two situations were distinguished within each class; one where only the query is removed from the database (top line) and another where the whole family was removed from the database (bottom shadowed line).

and $\alpha + \beta$ is understandable taking into the fact that both have successions of helical and sheet regions. Performance for identifying small proteins was equivalent to $\alpha + \beta$ class with rates of 65.3%–89.8%. Other two classes have very contrasting results based on the jack-knife procedure; when whole family is removed, probability to get true class as Top 1 hit drops from 72.8%–78.6% to 20.2%–37.8% for membrane and multidomain proteins. Multidomain proteins are mostly confused with $\alpha\beta$ class while membrane proteins, as expected, are mostly confused with α class.

Computation of class recognition matrix, for example, confusion matrix, using large number of domains highlights the efficiency of PB alignment. Decent efficiency rate is an indication that reduced complexity of 3D space and absence of topological information in PB representation has not affected the discriminatory power of PB alignment. This efficiency level can be attributed to combination of PBs connecting similar SSEs in different topologies (see below).

Efficiency rate within SCOP classes

Each class was studied separately to quantify how success rate at fold, super-family, and family was distributed within each class. Table V gives success rate for seven major SCOP classes, namely α , β , $\alpha\beta$, $\alpha + \beta$, multidomain, membrane, and small proteins, when whole family related to the query was removed or when only the query was jack-knifed.

Success of finding true fold among Top 10 hits was best for β and $\alpha\beta$ class with an efficiency of 71.1%–93% and 64.9%–92.2%, respectively, followed by membrane (87.8%–90.7%), small (66.7%–89.4%), $\alpha + \beta$ (66.5%–

87.5%), and α (62.3%–86.7%) class proteins. Similar trend was followed at super-family and at family level. Looking at hits that ranked first, β and $\alpha\beta$ classes achieved 53.8%–88.7% and 48.9%–87.8% of success, respectively, in finding true fold compared to α class where 45.2%–77.1% efficiency was reached. Presence of long helical regions in α proteins can be one of the reasons for more confusion among various folds in α class (as illustrated in the following discussion). Interestingly, distribution of success rates at three SCOP levels very well indicate that true hits at fold and super-family levels are not only populated by family members. These results are on same line as observed in Table III. Analysis of above results indicate that PB alignment is able to locate structure similarities even at very low sequence similarities (super-family relationships), and thus our method can be used to detect remote homologs for a given protein.

Closer look at the cases of failure where query protein was not able to find its true fold, super-family, or family within Top 10 ranks gave insight to current limitations of structure mining. Presence of single member folds, super-families, or families in database was most common contributor to absence of true hit. In some instances, diversity within family both in terms of length and structural features makes it difficult for the GA algorithm to extract true member. For example, ABC transporter protein from *Sulfolobus solfataricus* (SCOP domain d10xsc1) from MOP-like super-family (SCOP code b.40.6.3) is almost 40 residues longer than rest of the members. In this case, GA algorithm has to introduce large number of gaps to accommodate shorter proteins from the same family resulting in low alignment scores hence low rank. Application of LA provides an alternative solution in this

Table V

Efficiency Rate of Mining Similar Structure Proteins Within Each SCOP Class

	Only query domain was removed from database			Whole family related to query was removed from database		
	Top 10	Top 5	Top 1	Top 10	Top 5	Top 1
α (1337)						
Fold	86.7 (1160)	84.3 (1128)	77.1 (1031)	62.3 (833)	56.0 (749)	45.2 (604)
Super-family	83.2 (1113)	81.4 (1089)	74.4 (995)	69.8 (933)	64.4 (862)	56.6 (757)
Family	77.4 (1035)	75.0 (1002)	67.0 (922)	n/a	n/a	n/a
β (2077)						
Fold	93.0 (1931)	91.8 (1907)	88.7 (1842)	71.1 (1478)	66.3 (1378)	53.8 (1118)
Super-family	90.0 (1869)	88.8 (1844)	85.8 (1782)	70.5 (1464)	65.1 (1353)	53.3 (1108)
Family	87.2 (1812)	86.0 (1786)	83.1 (1726)	n/a	n/a	n/a
$\alpha\beta$ (1387)						
Fold	92.2 (1279)	91.2 (1265)	87.8 (1218)	64.9 (901)	58.5 (812)	48.9 (679)
Super-family	90.0 (1248)	89.0 (1234)	86.1 (1195)	63.4 (880)	57.0 (791)	48.8 (678)
Family	83.3 (1156)	82.6 (1146)	80.0 (1110)	n/a	n/a	n/a
$\alpha + \beta$ (1529)						
Fold	87.5 (1338)	85.7 (1310)	81.9 (1253)	66.5 (1017)	59.9 (916)	51.5 (788)
Super-family	84.3 (1290)	82.6 (1264)	79.2 (1211)	69.8 (1068)	65.0 (995)	59.7 (913)
Family	79.8 (1220)	78.3 (1198)	74.9 (1145)	n/a	n/a	n/a
Small (700)						
Fold	89.4 (626)	85.8 (601)	73.8 (517)	66.7 (467)	61.7 (432)	47.1 (330)
Super-family	84.7 (593)	80.8 (566)	70.6 (494)	61.5 (431)	58.2 (408)	49.0 (343)
Family	79.4 (556)	76.8 (538)	66.4 (465)	n/a	n/a	n/a
MultiDom (89)						
Fold	86.5 (77)	86.5 (77)	85.3 (76)	66.3 (59)	66.3 (59)	64.0 (57)
Super-family	86.5 (77)	86.5 (77)	86.5 (76)	66.3 (59)	66.3 (59)	64.0 (57)
Family	76.4 (68)	76.4 (68)	76.4 (68)	n/a	n/a	n/a
Membrane (140)						
Fold	90.7 (127)	87.8 (123)	80 (112)	87.8 (123)	85.0 (119)	67.8 (95)
Super-family	75.7 (106)	73.5 (103)	69.3 (97)	88.5 (124)	88.5 (124)	85.7 (120)
Family	73.5 (103)	71.4 (100)	67.8 (95)	n/a	n/a	n/a

Efficiency is calculated at three different ranks top 10 hits, top 5 hits, and 1st hit. Figures within brackets show the total number of queries taken into account or number of true hits, e.g., small (700) means in total we did this exercise for 700 proteins domains. Efficiency presented is in percentage, i.e., true hits/(true hit + false hit). n/a: not applicable.

case and enabled to extract at least one member protein in top hits. Human hyperplastic discs protein (SCOP domain d1i2ta_) from PABC (PABP) domain family (SCOP code a.144.1.1) is another such example where LA was able to extract true hit among top ranks and GA was unsuccessful. Note should be taken that not in all such cases success is achieved by LA approach. For example, Haloarcula marismortui protein (SCOP domain d1jj2s) from Ribosomal proteins L24p and L21e family (SCOP code b.34.5.1) is one such example where both diversity in structural features and protein length plays a role in unsuccessful results. Such examples are challenging and provide an opportunity to refine and improve our approach.

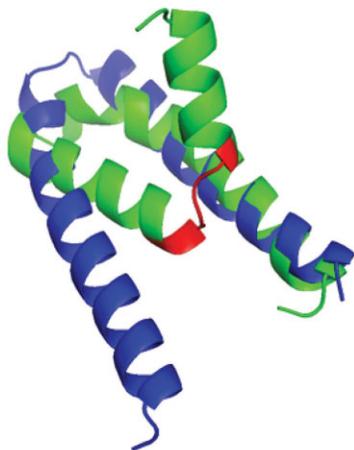
Furthermore, PB alignment technique had some problems with the pair of proteins sharing long stretch of regular secondary structures, for example, long helices in α proteins. In PB sequence, these regions are represented as long stretch of PB *m*; alignment of such regions artificially contributes to the global score and put them in high rank. This example is very well illustrated from pairwise alignment of ribosomal protein L12 from *Ther-*

motoga maritima (SCOP domain d1dd3a1) and ROP protein from *E. coli* (SCOP domain d1b6q_).

Figure 2 shows good alignment of helical regions (sequence of PB *m*), major reason for having high alignment score. Closer look at alignment indicates presence of extra loop in domain d1dd3a1, which is absent in other protein. Detection of this extra loop in one protein can hint in the difference in relative orientations of helices in two proteins even though the alignment score is high and is evident from Figure 2. This example highlights that sometimes alignment score can be misleading due to the high content of regular structures in two proteins but closer look into PB alignment can give clues to the structural differences. In such cases, disadvantage of 1D representation can be overcome by having a manual inspection to detect local variations present in-between regular structures.

Comparison with existing methods

Performance of PB-ALIGN has been tested against 13 structure comparison methods (Table VI). We applied



```
d1dd3a1#A ZZKLMHHHHHHMPCFKLMHHHHHHHHHHO FKLHHHHHHHHHHHHHHHHHHHHHHOZZ
d1b6q__#_ ZZKLMHHHHHHHHHHHHHHHHHHHHMPCFKLMHHHHHHHHHHHHHHHHHHHHHHH-ZZ
```

Figure 2

PB alignment-based superimposition of SCOP domain d1dd3a1 (green) and d1b6q__ (blue). PB alignment illustrates how long successions of PB m can contribute to alignment score. Presence of extra loop in protein 1DD3 is indicated in red color. It shows how small variation at local level can bring change in orientation of regular structures. Structural alphabet notation was explained by de Brevern et al.^{37,38}

batteries of tests to PB-ALIGN to obtain a comprehensive comparison with existing methods which included general efficiency of the method to extract-related proteins, ability to identify difficult structure similarities in database search, performance to handle multidomain proteins, and comparison with flexible structure alignment method like FATCAT. Evaluation results of existing methods are taken from recent studies done by Novotny *et al.*³ and Carpentier *et al.*,¹⁰ where 12 structure com-

parison methods were evaluated. Comparison with flexible structure alignment method is based on results produced by Ye *et al.*,³⁰ where 10 difficult pair alignments are compared between VAST, DALI, CE, and FATCAT. Dataset of 61 queries to compare general ability to extract related proteins and two multidomain protein queries are taken from the study done by Novotny *et al.* We followed same evaluation procedure as done by Novotny *et al.* and Carpentier *et al.* with one basic difference, both the studies followed CATH⁶ classification for test dataset and in our study we have used SCOP² classification for evaluation procedure. This has been done because PB-ALIGN uses database of SCOP domains filtered at 95% identity and many times there are differences in both classification schemes. A hit is counted as true hit if it belongs to same SCOP super-family or family level. It should be noted that some of the methods involved in this comparative study use significance threshold for the scores obtained to discriminate same fold from different folds but not all. However, our method is not initially based on the definition of a threshold measure and considers top hits in every mining exercise to evaluate the relative performance of methods. Nonetheless, measures have been developed to assess significance of the alignments (see paragraph cut-off below for details). Thus, we applied here similar protocols to Novotny *et al.* that have used few hits to compare those methods, which did not return the significance of hits.³

From our initial tests, we found out that by using complete protein chain as query, that LA algorithm gives far better results when compared to GA technique. This is obvious from the fact that many times protein chains are longer than actual domain boundaries and using GA in such cases increases number of gaps in alignment procedure. To avoid above pitfalls, we have used LA for our analysis.

Table VI

Structure Mining/Comparison Methods Tested in the Present Study

Program	URL	Methodology used
CE	http://cl.sdsc.edu/ce.html	Inter residue distances
DALI	http://www.ebi.ac.uk/dali	C α distance matrices
DEJAVU	http://xray.bmc.uu.se/usf/dejavu.html	SSEs comparison
FATCAT	http://fatcat.ljcrf.edu/	RMSD and introduction of twists
LOCK	http://brutlag.stanford.edu/lock2	RMSD minimization
MATRAS	http://biunit.aist-nara.ac.jp/matras	Markov transition model
PB-ALIGN	http://bioinformatics.univ-reunion.fr/PBE/PBE-ALIGN.htm	PBs substitution matrix and alignment
PRIDE	http://hydra.icgeb.trieste.it/pride	C α distance distribution
SSM	http://www.ebi.ac.uk/msd-srv/ssm	SSEs vector comparison
TOP ^a	http://bioinfo.mbfys.lu.se/top	SSEs alignments
TOPS	http://balabio.dcs.gla.ac.uk/tops/compare.html	SSEs symbolic representation and comparison
TOPSCAN	http://www.bioinf.org.uk/topscan	SSE representation in topology strings, aligned through a global dynamic alignment algorithm
VAST	http://www.ncbi.nlm.nih.gov/Structure/VAST/vastsearch.html	SSEs graph representation
YAKUSA	http://www.rpbs.jussieu.fr/yakusa	Internal coordinates matching

^aWeb link unreachable.

Using LA, we queried each protein chain against the databank and compiled results simply by counting if true hit is found within Top 10 alignments, number of members found in Top 10, and rank of 1st false positive. Alignments are ranked based on score generated by LA algorithm plus normalized and Z scores are also reported for each hit. Out of 61 queries, we found two cases (1rlr and 1vmo) had no super-family and family members in our databank except themselves. In total, we tested 59 test cases for general efficiency of the method and compared our results with the results reported by Carpentier *et al.* (Table VII). Overall PB-ALIGN performed with a success rate of 96.6% when Top 10 ranking alignments are considered.

Our method performs correctly in all except two cases. Toxin protein 1ciy (PDB id) from *Bacillus thuringiensis* has three domains, namely δ -Endotoxin C terminal, middle and N terminal domain. PB-ALIGN is able to extract C terminal and N terminal domains very easily in top hits but misses out target middle domain (SCOP code b.77.2.1) of 1ciy from initial hits and is found only at 48th rank. Because of low rank in hits, we have counted this hit as negative in our final results. Second protein 1gj (PDB id) from *E. coli* has two domains and target domain (GreA transcript cleavage protein, C terminal domain, SCOP code d.26.1.1) is present as lone member of family in our database. PB-ALIGN is not able to identify target family (single member family) or super-family members among top hits. Target super-family members are obtained at 12th and 16th rank if mining is performed with gap penalty of -3.0 . Our assessment also found out that for only five queries out of 59 tested, the rank of first false positive was above the rank of true hit and there was not a single case where first true positive was ranked after a false hit. Moreover, time taken to query each protein was less than a minute, making it one of the fastest and efficient structure comparison method among the 13 methods (see Table VII) evaluated in present study.

Performance of PB-ALIGN on nontrivial dataset

We further tested our method's performance on a non-trivial dataset used by Carpentier *et al.*,¹⁰ which is constituted of 14 difficult cases. We queried each protein using both LA and GA algorithm against our database and considered first 100 alignments as well as a cut-off score value of -0.25 for GA (see below). Results of this exercise are comparable with previous data published by Carpentier *et al.*¹⁰ On this limited dataset, PB-ALIGN performance was found to be at par with YAKUSA and CE and gave about 50% success rate with combined effort of LA and GA algorithm. However, the efficiency of PB ALIGN as a pairwise comparison tool still needs to be assessed in an in-depth benchmark in comparison

Table VII

Comparison of PB-ALIGN With Existing Structure Mining/Comparison Methods

Program	Mainly α (19)	Mainly β (19)	Mixed $\alpha\beta$ (15)	Few SSEs (8)	Total (%)
PB-ALIGN	18 ^a	17 ^b	14	8	96.6
YAKUSA	17	19	14	8	95
CE	17	19	13	8	93
DALI	14	19	14	8	90
MATRAS	11	19	14	8	85
VAST	12	17	15	7	84
TOP	14	18	12	7	84
DEJAVU	14	19	9	4	75
TOPSCAN	15	12	9	7	70
TOPS	2	15	14	7	62
PRIDE	14	14	7	3	62
LOCK	0	14	11	8	54
SSM	5	13	10	5	54

Comparison of PB-ALIGN with 12 structure mining/comparison methods based on results from Carpentier *et al.*¹⁰ The numbers along with the header give total number of queries belonging to each class. All the hits are counted based on first 10 ranking alignments compared to 100 hits taken by Carpentier *et al.*, only for those methods that did not return the significance of hits.

^aOne query has no target in our database.

^bFor mainly β class, query protein 1vmo has no target in our database and query 1ciy misses target in top ten ranks.

with extensively tested, robust and standard methods such as CE, DALI, and VAST. Nevertheless, testing of both LA and GA approach on nontrivial dataset gave very interesting insight of our method. LA algorithm was able to get only four targets out of the 14 tested, whereas GA found a total of six targets with three extra hits from LA results and missing out one case found by LA. Table VIII gives the summary of results obtained using both the approaches. Application of GA not only identified more number of difficult targets but also improved the rank of target in two cases (Table VIII). When cut-off value (see next section) is applied as a rule for decision, GA is able to capture seven targets above the threshold value. Like YAKUSA, PB-ALIGN uses local structural features to describe and encode protein backbone, and identifying distantly related proteins can be difficult due to the fact that such pairs share structural similarities at global level rather than local level. Ability of PB-ALIGN to use GA algorithm to capture such remote similarities at global level using local descriptors (PBs) sets it apart from methods like YAKUSA.

Test case 1crb and 1bge from mainly- α class demonstrate this fact very clearly by analyzing GA of query (1crb) and target (2gf) protein PB sequences as shown in Figure 3(a). Using GA, we were able to find target for query protein 1crb among top hits with low alignment score. Looking at PB alignment, it becomes very obvious why LA method was not able to capture these global similarities. Both the proteins share four helical regions (populated by PBs *m*) separated by loops and small strands (populated by PBs *c* and *d*) and two middle helical regions are of different length. Such global similarity

Table VIII

Performance of Local and Global Alignment Algorithm on Nontrivial Dataset

Query protein	Target protein	Local alignment	Global alignment	Cut-off value on GA alignment
1aep	256b:A	0	0	0 (-0.29)
2mta:C	1ycc	0	0	0 (-0.74)
1rcb	2gmf:A	0	1 (48) ^a	1 (+0.02)
1bge:B	2gmf:A	0	0	0 (-0.34)
2afn:A	1aoz:A	1 (10) ^b	0	0 (-0.48)
3hla:B	2rhe	0	0	1 (+0.23)
2aza:a	1paz	0	0	0 (-0.29)
1cew:l	1mol:A	0	1 (59) ^a	1 (-0.06)
1dsb	2trx:A	0	0	0 (-0.68)
1fxi:A	1ubq	1 (42)	1 (28) ^c	1 (+0.26)
3chy	2fox	0	1 (33) ^a	1 (+0.18)
1gpl	2trx:A	0	0	0 (-1.94)
1hip	2hip:A	1 (6)	1 (7)	1 (+0.56)
1isu:A	2hip:A	1 (59)	1 (15) ^c	1 (+0.14)

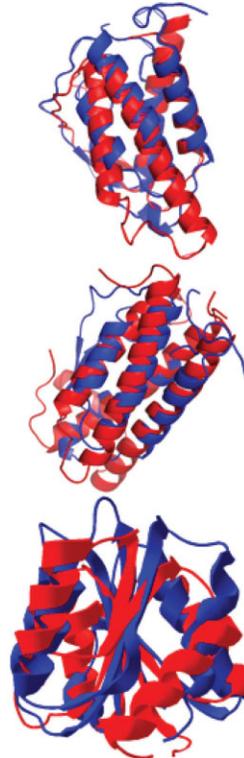
In total, both methods were able to find seven target proteins. Success and failure of GA and LA is indicated by 0 (failure) and 1 (success). Here, target rank is indicated within parenthesis. Success of GA based on the application of a cut-off value of -0.25 is also indicated by 0 if score < -0.25 (failure) and 1 if score is > -0.25 (success). Values within parentheses are the normalized alignment score (see text for details).

^aTarget exclusively found by GA.

^bTarget protein missed by GA.

^cImprovement in rank using GA.

can only be captured by GA algorithm having lower gap penalty compared to high penalty imposed by LA approach. Use of simple GA algorithm combined with PB substitution table highlights subtle similarities identified by PB-ALIGN method based on local backbone descriptors (PBs). Figure 3(b) also shows a query protein (1bge) for which target protein (2gf) was not found even after using GA. Close inspection of PB alignment reveals four helical regions are well aligned despite the differences in helix length. Presence of many gaps to obtain this alignment results in very low alignment score, which pushed down the pair below the top hits. Another example where target (2fox) was found by using GA is query protein 3chy from mainly- $\alpha\beta$ class; Figure 3(c) shows superimposition of 3chy and 2fox from ProFit based on global PB alignment. Once again identification of such similarities is not possible by using LA techniques due to the presence of variable regions and has to be accommodated by gaps in an alignment. The above results show that the possibility to align PB sequences using local or GA techniques offers flexibility to recognize both strong local similarity and distant (variable) global similarities shared by proteins.

**Figure 3**

Global alignment of PB sequences. (a) PB sequence alignment and superimposed structures for protein pair 1rcb and 2gfA. Target protein 2gfA is found after using GA. (b) PB sequence alignment and superimposed structures for protein pair 1bgeB and 2gfA. GA fails to find target protein 2gfA. (c) Superimposed structures of 3chy and 2fox based on GA of PB sequences. Structural alphabet notation is explained in de Brevern et al.^{37,38}

Table IX

Comparison of PB-ALIGN and FATCAT

Protein 1	Protein 2	VAST	DALI	CE	FATCAT	PBALIGN	ProFit
1fxiA	1ubq_	48 (2.1)	60 (2.6) ^a	64 (3.8) ^a	63 (3.01)	59 (2.6)	55 (2.0)
1ten_	3hhrB	78 (1.6)	86 (1.9)	87 (1.9)	87 (1.9)	82 (4.1)	84 (4.0)
3hlaB	2rhe_	—	63 (2.5)	85 (3.5)	79 (2.81) ^b	67 (2.4)	73 (2.6)
2azaA	1paz_	74 (2.2)	81 (2.5) ^a	85 (2.9)	87 (3.01)	79 (2.3)	79 (1.9)
1cewl	1molA	71 (1.9)	81 (2.3)	69 (1.9)	83 (2.44)	74 (2.5)	16 (2.5)
1cid_	2rhe_	85 (2.2)	95 (3.3)	94 (2.7)	100 (3.11)	87 (2.2)	25 (2.9)
1crl_	1ede_	—	211 (3.4)	187 (3.2)	269 (3.55) ^b	179 (2.3)	75 (2.9)
2sim_	1nsbA	284 (3.8)	286 (3.8)	264 (3.0)	286 (3.07)	262 (2.4)	264 (2.4)
1bgeB	2gmfA	74 (2.5)	98 (3.5)	94 (4.1)	100 (3.19)	90 (2.4)	88 (2.4)
1tie_	4fgf_	82 (1.7)	108 (2.0)	116 (2.9)	117 (3.05)	105 (2.2)	104 (2.1)

Comparison of various methods based on number of residues aligned and *rmsd* (within brackets) obtained for 10 difficult examples based on global alignment. Results for other methods is taken from Ye *et al.*³⁰

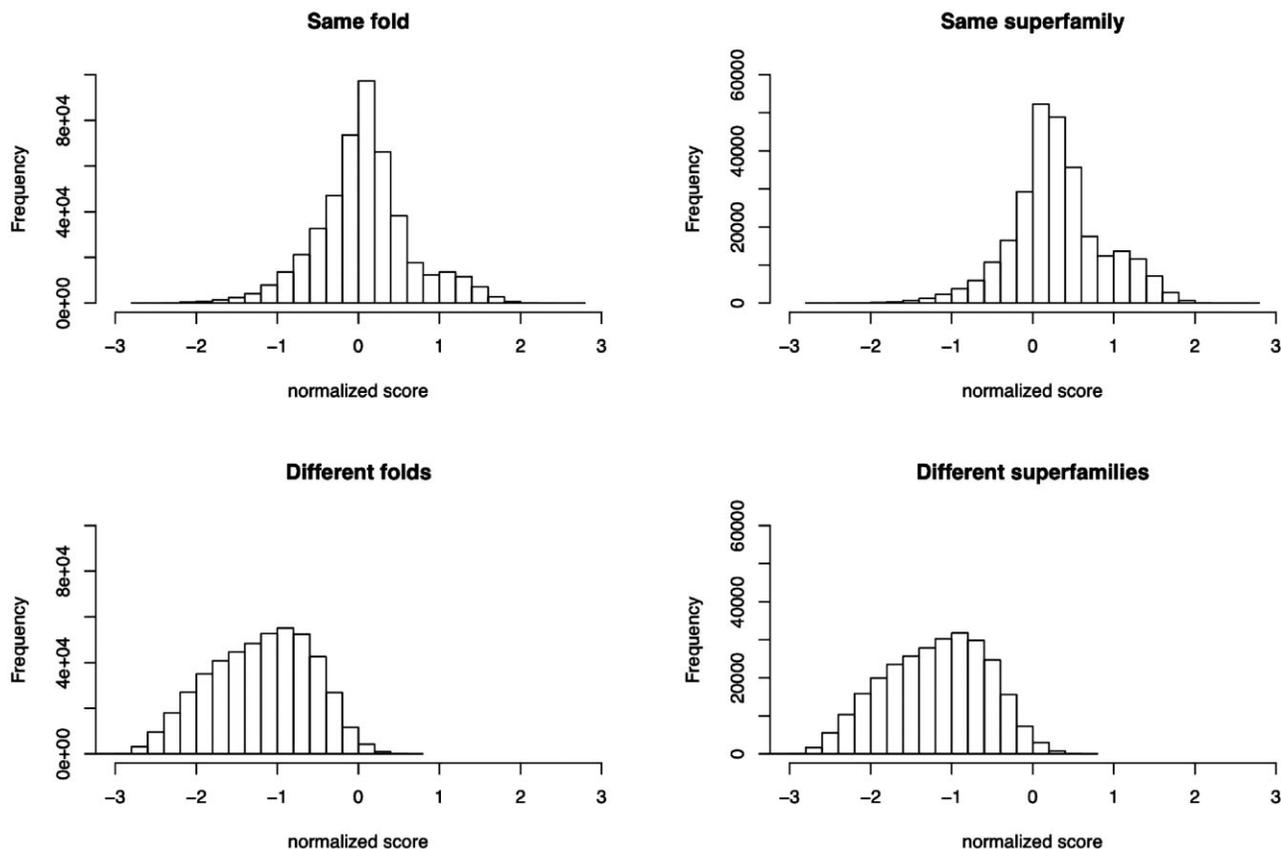
^aNo results obtained in previous study done by Ye *et al.*³⁰

^bFATCAT introduced twists in structures to perform superposition.

Protein 2afn was the only query where LA outperformed GA. Prime reason of GA failure can be understood from the fact that query protein chain 2afnA contain multiple domains, and GA against our database will need to introduce large number of gaps resulting in low alignment score, whereas in case of LA algorithm only probe and target domains are aligned with high alignment score. These results indicate usage of GA algorithm on sequence of PBs (encoding local structure variations) is better suited to situations where structural similarities are shared at global level and are difficult to obtain with LA techniques. In situations, where protein chains are suspected to contain multiple domains or one protein structure is completely or partially contained in other protein, LA approach proves more advantageous.

GA of few difficult pairs showed at global level that the method was able to align equivalent regions in two proteins, but due to the low scores, such pairs were missed altogether by database search approach. We extended above analysis by studying pairwise alignment of tough cases and compared alignment results with flexible alignment method called FATCAT. We selected 10 difficult pairs used by Ye *et al.* and compared PB-ALIGN with VAST, DALI, CE, and FATCAT based on number of residues aligned and superposition *rmsd* obtained. Table IX shows number of residues aligned along with *rmsd* values (within brackets) based on GA of PB sequences. Other methods are compared based on the results obtained by Ye *et al.* In our case, superposition of two proteins was done using ProFit based on alignment provided by PB-ALIGN and further iterations were performed by ProFit to obtain final results. In other words, results presented in Table IX are combined effort of PB-ALIGN and ProFit. To measure the contribution of ProFit, we also performed another exercise where superposition was performed based on sequence alignment generated by ProFit to define initial equivalent zones and carried out iteration from there on to get final values.

Results we obtained are very interesting, since ProFit alone by itself gave comparable results to FATCAT and PB-ALIGN in 7 out of 10 cases. Remaining three pairs (1cewl, 1molA; 1cid_, 2rhe_; 1crl_, 1ede_) gave much improved results when combined with PB-ALIGN. This outcome has two implications: first, ProFit by itself is good enough superimposition method to superimpose protein pairs sharing low sequence similarity and can achieve comparable results to more complex and robust methods; second, in the cases where ProFit fails to find optimal results by simple amino acid sequence alignment, PB alignment provides good starting points to ProFit, unidentifiable by sequence alignment alone. In all ten cases, PB-ALIGN coupled with ProFit gave desirable results compared to other complex methods. When compared to a flexible alignment and superimposition method FATCAT, PB-ALIGN gave low *rmsd* in most of the cases with slightly less number of residues superposed. It is noteworthy that methods like FACAT has real advantage in this study where it introduces twists in structures to superimpose more residues with low *rmsd* and despite this advantage our simple methodology gave decent results. The only test case (pair 1crl_, 1ede_) where PB-ALIGN produces significantly lower results compared to FATCAT can be understood from the fact that five twists were introduced in protein structure to superimpose 269 residues with a *rmsd* of 3.55 Å. In its present form, though PB-ALIGN will align PB sequences in a flexible manner, it is still not capable to produce such results as it relies on rigid body superposition method. Objective of this analysis was not to compete with methods like FATCAT (which we believe in principle will give better results specially in cases where twists are needed to superpose structures) but it is to highlight, (i) despite using very simple approach, PB alignment technique gives comparable results in most of the situations with minimum computation time making it practical for large scale analysis in real life situations and (ii) premises

**Figure 4**

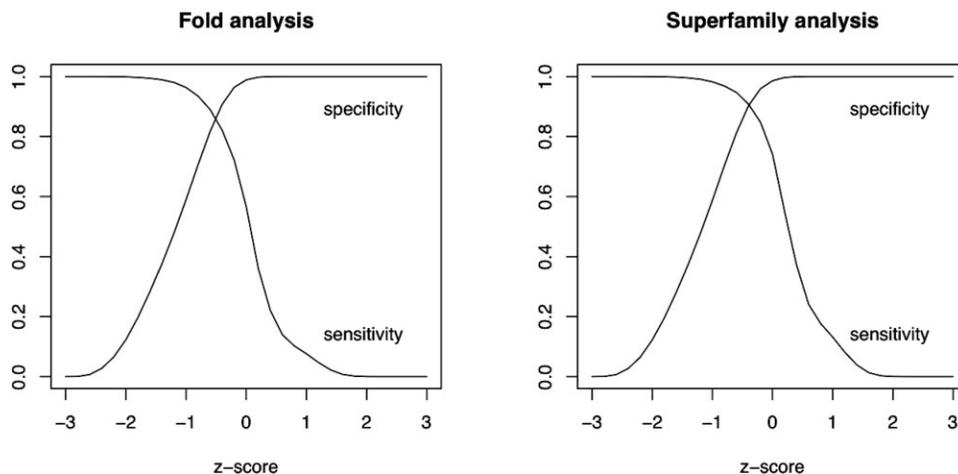
Distribution of normalized scores after PBs alignment between pairs of proteins from the same fold or super-family (top) and from different folds or super-families (bottom).

for flexible structural superimposition as performed by FATCAT are featured in the method of PB alignments owing to the nature of the algorithm used.

Handling of multidomain proteins

PB-ALIGN was also tested on two multidomain proteins, 2src_ and 2hckA (human Src and Hck kinase proteins, respectively), to assess efficiency of method to handle protein chains containing multiple domains during database search. The database used in our case is a collection of domains on SCOP classification; hence, it was calculated whether the method is able to extract target domains among top hits. As seen above, LA technique has advantages over GA algorithm in such cases. Hence, in the present analysis, we used LA algorithm to extract different domains from database. Based on SCOP classification, query proteins are composed of three different domains, namely SH3 domain, SH2 domain, and protein kinases catalytic subunit. Our evaluation on mul-

tidomain proteins is slightly different from the earlier studies,^{3,10} where success was measured if hits contained all the four domains (based on CATH classification) followed by proteins having two or one domain. In our study, we assessed if all the domains (SH3 domain, SH2 domain, and protein kinases catalytic subunit based on SCOP definition) are present among Top 100 hits. Previous studies reported that YAKUSA, DALI, VAST, MATRAS, and CE gave best results while handling multidomain cases. SSM found proteins having all four domains, and TOP and DEJAVU found structures sharing more than one domain while having a blind eye to single domain structures. LOCK managed to find representative of each domain, but failed to find proteins having all domains in single chain. TOPSCAN, PRIDE, and TOPS were among least efficient methods. PB-ALIGN was able to find all three target domains among top hits. SH2 and kinases catalytic subunit domains were most easily found and were populated among top hits. SH3 domain was always found in at lower ranks (61st and 37th rank), and

**Figure 5**

Analysis of variation of sensitivity and specificity according to different cut-off scores.

this can be attributed to smaller length and high population of other two domains in our database.

Cut-off threshold for PB-ALIGN scores to recognize common folds

On the basis of various assessment exercises described above, we worked out a recommended threshold for the PB-ALIGN scores that will allow one to designate a hit in a structural database as same fold as that of the query. Figure 4 provides a distribution of scores of PB-ALIGN for the cases of common fold and different fold (according to SCOP). This figure shows that a region of scores is taken-up by proteins with the same fold as well as different fold. As fold space is a continuum, it will be difficult to have a precise score that will completely segregate same folds from different folds. We hence analyzed the variation of sensitivity and specificity for different normalized score thresholds (see Fig. 5). Because we want to typically minimize false positives while having an acceptable level of sensitivity (true positives), we propose to select appropriate cut-off at a stringent specificity value of 0.95. Hence on the basis of the aforementioned specificity value, the normalized score cut-off value was -0.250 and the sensitivity for proteins from the same fold was of 0.75. Similarly, for proteins from the same superfamily, the score cut-off value was -0.252 and a sensitivity of 0.87. Hence, we suggest a threshold value of -0.250 to discriminate between proteins from the same fold or same super-family. This cut-off works correctly for demarcation of same folds or super-family from different folds or super-family although not for all the cases. Going by this argument cut-off, a total of 75% and 87% of the proteins with the same fold and super-family as

the query, respectively, are correctly picked-up by PB-ALIGN. Importantly, rate of false hits is only of 5% in both situations.

Understanding whether the observed PB sequence similarity is just a chance event is the central problem for the evaluation of the statistical significance of alignment scores. The basic question to be answered is what is the probability that a similarity score as great as that actually observed between real sequences could have arisen by chance, when sampling from suitably-defined populations of unrelated sequences? To address this question, the distribution of GA scores from real but unrelated sequences

Table X

Estimates of Extreme Value Distribution Parameters for Alignment Scores Between Real but Unrelated Sequences of Different Sequence Length Subsets (See Also Fig. 7)^a

Length (number of residues)	Shape parameter (ξ)	Scale parameter (σ)	Location parameter (μ)
40	0.376	0.673	0.993
70	0.359	0.539	0.831
100	0.368	0.506	0.774
130	0.349	0.418	0.685
160	0.397	0.353	0.621
190	0.406	0.384	0.644
220	0.416	0.354	0.599
250	0.424	0.358	0.535
280	0.444	0.337	0.480
310	0.402	0.261	0.519
340	0.435	0.278	0.540
370	0.456	0.262	0.520
400	0.477	0.242	0.499

^aThese parameters were derived using *gev* function in *evir* package implemented in R statistical software.⁵¹

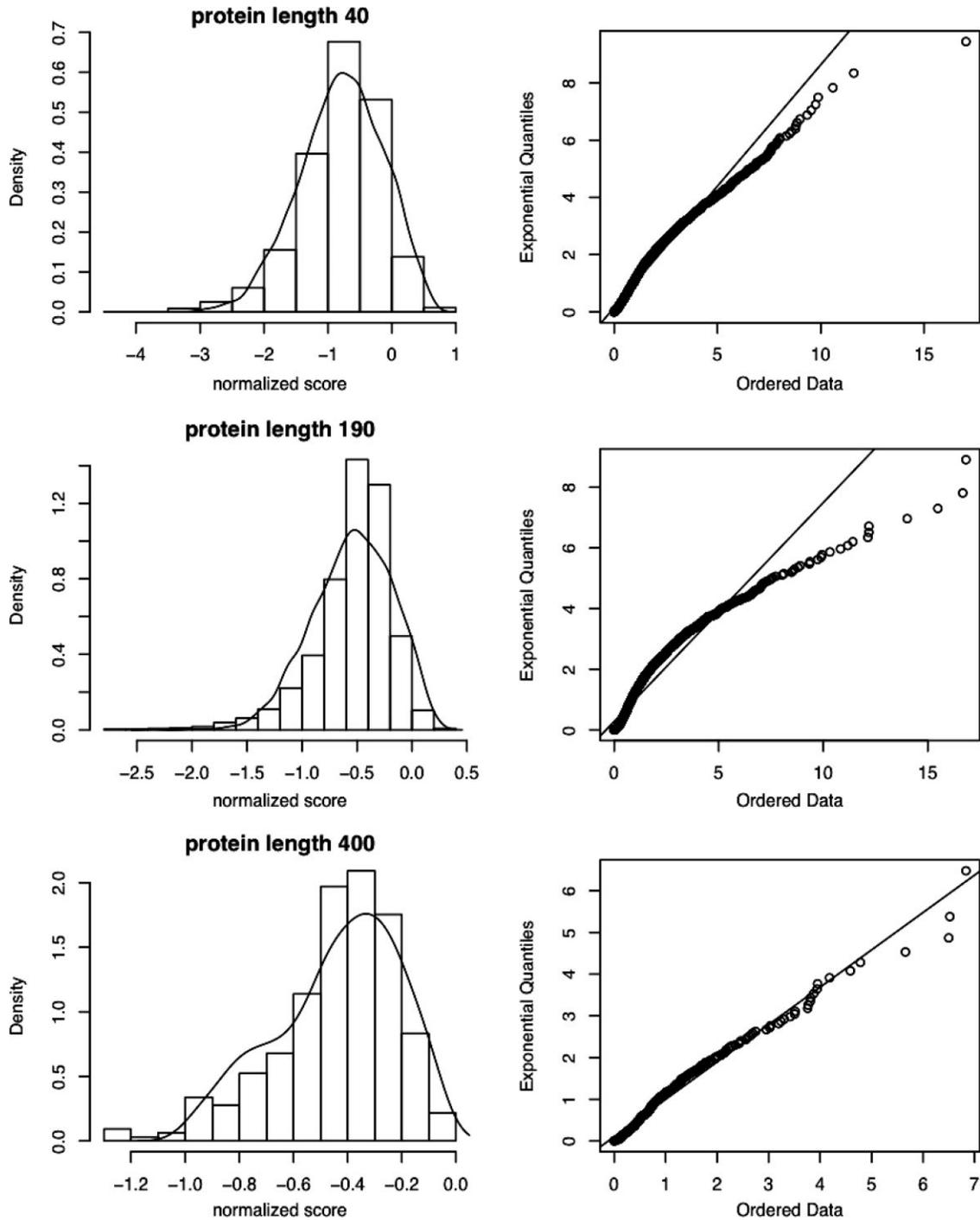


Figure 6

Distribution of scores from global alignments of real but unrelated sequences (RUSs) datasets of 40-aa, 190-aa, and 400-aa long. The distribution of the scores was estimated with extreme value distribution curve indicated in solid line using *evir* package from R statistical software.⁵¹ On the right are displayed the corresponding quantile plots.

for different length subsets (40-aa through 400-aa by 30-aa increment, see also Table X) need to be analyzed. As shown for three examples in Figure 6, alignment scores

were distributed according to an extreme value distribution (EVD). We hence derived all three corresponding EVD parameters (Table X), which could be used to mea-

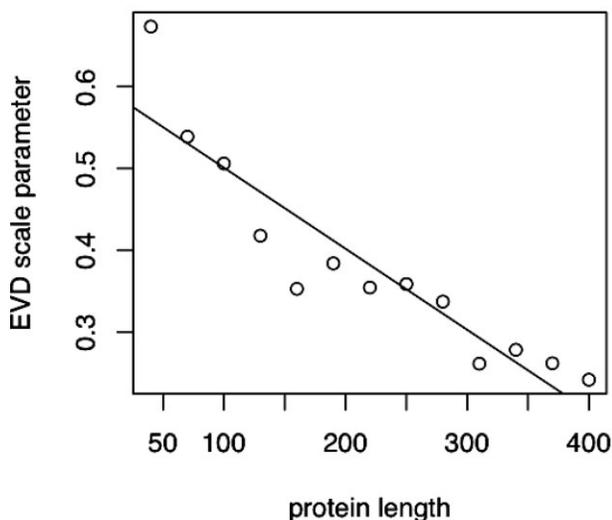


Figure 7

Variation of estimates of EVD scale parameter (σ) with length of protein sequences calculated from global alignments of real but unrelated sequences (RUSs) datasets (see Table X). Fitted regression line with $R^2 = 0.85$ ($P < 0.0001$) as shown in solid line was calculated using *lm* function from R statistical software.⁵¹

sure confidence of alignment scores to classify two proteins as having the same fold or belonging to same super-family. The scale parameter (σ) linearly decreased with length alignment, which further comforts the inferred EVD distribution model (see Fig. 7).

CONCLUSIONS

In the era of structural genomics, protein structure comparison and mining plays an important role in computational biology. Identification of new phylogenetic relationships, functional annotation, and study of sequence to structure relationships are some of its most common targets. In this study, we have presented a new structure mining method called PB-ALIGN, based on the encoding of protein backbone as sequence of short local motifs (PBs) and their alignment using a newly derived PB substitution matrix and simple dynamic programming. The method is simple and is scalable for large scale analysis and provides an alternative tool for structural genomics. Use of local structural features (PBs) to describe protein backbone and alignment of such features provides an alternative to previously known methods like DALI and CE for mining protein domains. Existing methods rely on SSEs' information for structure alignment and misses out on large amount of structural information beside regular structures in proteins. PB representation of protein backbone highlights subtle variations and structural conservations present beyond local regular structures, for

example, N and C caps of helices and strands. Capability of PB-ALIGN to align these regions is a step ahead of existing methods.

The method is performing reasonably well in mining structurally similar proteins from large database at both fold and super-family level. Among peer comparison, PB-ALIGN stood out at par with other methods to mine structures and at best in terms of speed. Ability to obtain good mining capacity at high speed highlights the simplicity and effectiveness of the method. Generally speaking, the efficiency of PB ALIGN as a pairwise comparison tool still needs to be assessed in an in-depth benchmark in comparison with extensively tested, robust, and standard methods such as CE, DALI, and VAST. Nevertheless, compared to methods like YAKUSA that also relies on representation of local structural features, our method performed superior on general test data and at par on difficult (nontrivial) dataset. The main difference between these two methods is the final objective. YAKUSA aims to locate strong gap-free local structural similarities or "blocks"¹⁰ between two proteins and is not concerned with global similarities spread over protein length, whereas PB-ALIGN despite using local structural features aims to address both local and global similarity between proteins. Availability of PB substitution matrix and use of local or global sequence alignment techniques help to answer both local and global structure similarities. Both alignment techniques are shown to be useful in different conditions, for example, LA is beneficial if one wants to identify strong local similarities or if protein chain is multidomain or if one protein is completely or partially included in other structure. GA is useful if two proteins share structural similarities spread across protein length. Our experience suggests that user should use both local and GA feature, and manual inspection of PB alignments will clearly highlight the best approach. Another advantage we found in PB-ALIGN is intuitive nature of PB alignment representing structure alignment, and many times, simple inspection of alignment gives hint about structural differences between proteins prior to 3D visualization.

Importantly, this study derived a score cut-off, for the inference of structural similarity between structural domains whose relationship is unknown using their PB representations. It further specified the extreme value distribution of GA scores of real but unrelated PB sequences. This information is currently being used to implement a statistical significance threshold in PB-ALIGN.

Comprehensive assessment of our methodology also highlighted some shortcomings and need of further fine-tuning of PB-ALIGN. At present, we have used simple dynamic programming and linear gap penalty. We believe use of more robust flavor of dynamic programming and change in gap penalty will further improve the alignment quality. Artificial increase in alignment score due to long stretch of regular structures especially in α class proteins

is also being looked into and change in scoring function is anticipated. Furthermore, we would like to introduce combined scoring function taking into account number of aligned residues, rmsd value, and alignment score. We believe that the use of PB alignment methodology to perform multiple alignment of family members would enable use to define “core” structures having boundaries beyond SSEs and would help in finding distant homologues. PB-ALIGN is also expected to be useful in homology modeling and loop modeling.

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